Local Call Admission Policies for Cellular Networks Using Genetic Algorithms

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Abstract

It is well known that if a stochastic service system (such as a cellular network) is shared by users with different characteristics (such as differing handoff rates or call holding times), the *overall* system performance can be improved by denial of service requests even when the excess capacity exists. Such selective denial of service based on system state is defined as call admission. A recent paper suggested the use of Genetic Algorithms to find near-optimal call admission policies for cellular networks. In this paper, we define *local* call admission policies that make admission decisions based on partial state information. We search for the best local call admission policies for one dimensional cellular networks using Genetic Algorithms and show that the performance of the best local policies is comparable to optima for small systems. We also test our algorithm on larger systems and show that the local policies found outperform the maximum packing and best handoff reservation policies for the systems we have considered.

1 Introduction

Allocating radio resources to users with minimum blocking of new calls and dropping of handoffs has become a vital issue in mobile communication system design. It is known that dynamic channel allocation schemes can reduce these blocking and dropping probabilities for a reasonable range of loadings [1][2][3]. However, allocating channels to every user whenever the sources are available may not be the optimal strategy in terms of system performance. The performance can be improved (or equivalently the blocking probabilities can be further reduced) by imposing a state-based call admission policy on a system where there are users with differing service characteristics. The problem then becomes one of finding the call admission policy that provides optimal system performance.

The call admission problem has been studied extensively in the context of multirate circuit switching in [4] [5] [6] [7] [8]. Call admission to a single cell has been considered in [9]. In all cases, optimal policy search assumes an underlying Markov Process model and uses Dynamic Programming (Markov Decision Processes-MDP) to find the optimal policy. Unfortunately, issues such as state-space size often render MDP impractical.

In recent work [10] we used Genetic Algorithms (GA) to find near-optimal call admission policies in cellular networks to overcome the computational limits of MDP approach. In this paper, we extend the approach by considering call admission with incomplete state information. Specifically, we consider admission policies for one dimensional cellular networks using only *local* rather than global channel occupancy information. The optimization problem based on local state is no longer Markovian and the MDP approach cannot be used directly.

Section 2 describes the network and the optimization problem. Section 3 defines local state-based policies and is followed by Section 4 which considers the application of GA to the local call admission problem. In section 5, we first test the algorithm on a small system and compare the performance to optima located using MDP. We then apply GA to a larger system and compare our results to well-known allocation techniques such as maximum packing and handoff reservation policies.

2 Problem Definition

Consider a one-dimensional ring structured network with an even number of cells. We assume channel reuse such that a channel can only be used once in any K mutually interfering cells (cliques). It has been shown that a valid channel assignment scheme can be found for such systems if all cliques have occupancy less than or equal to C [11]. We further assume that channel reassignment is always possible if needed.

Consider then a system with two types of service requests, i.e. new call set up request and handoff request. We assume a Markov model in which the new call arrival process to cell i is modeled as Poisson with rate

$\lambda_i = \lambda$. Call holding times are exponential with average call completion rate $\mu_i = \mu$. We also assume that calls in progress are subject to handoff to either of the two neighboring cells, and the time a mobile user spends in cell i is exponential with rate $\gamma_i = \gamma$ (independent of the call arrival and call holding process).

We define the cellular system performance, T, as a linear combination of call dropping and call blocking;

$$T = P_b + \omega P_h \tag{1}$$

where P_b and P_h are the new call blocking and handoff dropping probabilities respectively, and ω is the *relative penalty factor*. This performance measure penalizes dropping of a handoff $\omega > 1$ times more than blocking a new call request; an intuitively reasonable assumption. The reader should note that with $\omega = 1$, the performance measure is simply the probability of unsuccessful call completion,

$$T = P_b + P_h = 1 - P_c \tag{2}$$

where P_c is the probability of successful call completion. P_c is defined as the probability of not being blocked or dropped over the lifetime of a call from setup request to natural call termination.

3 Local Policies

A call admission policy is a collection of admit/reject decisions corresponding to the services requested at each state of the system. It can be described as a binary mapping where the admit decisions are represented by 1's and rejections by 0's. These admit/reject decisions are assumed to be independent of the system constraints, i.e. although a policy may try to admit a service request when the system is full, service will be denied due to unavailability. This formulation circumvents to problem of policy feasibility since *all* policies are then feasible.

We define a *global* call admission policy as one which provides a decision for each state of the network. A global policy for the cellular system described in Section 2 provides the following decisions per cell per state:

- Admit/Reject a new call arrival
- Admit/Reject a handoff request from the right cell
- Admit/Reject a handoff request from the left cell

The size of the global call admission policy is then $3 \times N \times S$ bits, where N is the number of cells in the network and S is the number of feasible states of the system.

For practical systems, this size can be very large and may prohibit the use of MDP to find the optimal call admission policy. As an example, consider a 16-cell, 9-channel system. Since the number of states in the system is on the order of [1] $(C+1)^N$, the size of the policy is roughly 48×10^{16} bits. Furthermore, a global policy requires complete and up-to-date state information to be distributed to each cell. This may cause unacceptable signaling overhead for an already burdened signaling system[**?**].

An alternative approach is to define *local call admission policies* where decisions are based only on partial state information. In this case, a cell (base station) would only keep track of the state information from small number of cells and make decisions based on the abbreviated state information which we define as the *local state*. Policies defined on the local state are therefore much smaller. This in turn means the policy search space is much smaller and policy search is simplified.

Definition 1 *A local policy is said to have* locality k *if it uses the state information from its* $2k$ *nearest neighbors.*

Thus, a base station operating with a policy of locality k uses the state information from its k left and k right nearest neighbors as well as its own state. To further reduce policy complexity, we will assume a ring network and exploit its symmetry; i.e., the policy in each cell is assumed identical to that in other cells (within a spatial shift) [11]. The maximum possible state space then reduces to $(C+1)^{2k+1}$ states, and the length of the local policy becomes $3 \times (C+1)^{2k+1}$ bits per cell.

The locality conditions considered in this paper are $k = 0$ and $k = 1$. $k = 0$ corresponds to completely ignoring the state of adjacent cells whereas $k = 1$ corresponds to a local policy which uses the nearest neighbor state information in addition to self-state information. The above example with 16 cells and 9 channels needs only 30 bits for the policy with $k = 0$, and 3000 bits for $k = 1$.

It is worthwhile to restate that the search for optimal local policies is not amenable to MDP since the underlying state is no longer Markovian. Thus, genetic algorithms afford a systematic approach to a problem intractable using standard analytic methods. GAs perform surprisingly well in a variety of optimization tasks [12].

4 Genetic Algorithm Implementation

We use a typical two parent - two offspring Genetic Algorithm described in [10]. Each local policy represents an organism in GA terminology and is a collection of bits corresponding to admit (1) and reject (0) decisions for the new call set up and handoff requests at each *local*

[1] The given number is the number of states in the unconstrained state space, the number of feasible states is actually less due to reuse constraints.

state of the system. A group of local policies (a community) is chosen at random initially. Each policy in the community is evaluated (via Monte Carlo simulation) using Equation 1 as the performance measure. Policies with better performance are more likely to enter the *mating pool*. These so-called *parent* organisms perform crossover to exchange some bit information pairwise and result in offspring policies. Finally, offspring policy bits are inverted randomly (mutation).

After mating, policies are chosen for deletion with probability inversely related to their fitness. The offspring are then inserted into the population. In our implementation, the population of the community is kept constant from iteration to iteration; we only delete as many policies as there are offspring. This basic algorithm is repeated for some number of *generations* or until policy improvement appears to stagnate.

5 Results and Discussion

5.1 4-cell System

The algorithm was first tested on a small system for which optimal global call admission policies are available via MDP. The system has 4 cells on a ring, 4 channels available and is modeled with the new call and handoff service model described in Section 2.

In the first set of experiments, the traffic load of the system is fixed while the relative penalty factor ω for dropping handoff calls is varied. Specifically[2],

$$\lambda = \mu = \gamma = 1.0 \qquad \omega \in [1, 10]$$

The Genetic Algorithm is used to search for local call admission policies with $k = 0$ and 1 that minimize the performance measure given by Equation 1.

In Figure 1, we compare the resulting performances of the best local policies found by GA to the following:

- AIP: admit-if-possible (maximum packing strategy) where a service request is always granted unless it is impossible to assign the channel due to reuse constraints
- OPTIMAL: the optimal global policy performances found by MDP

As expected, weighted blocking for the AIP policy grows linearly with increasing ω. In contrast, the optimal policy weighted blocking rises rapidly and then more slowly. The GA with both $k = 1$ and $k = 0$ provides near-optimal policies for small ω and also outperforms AIP for higher ω. Surprisingly, even completely ignoring neighboring cells ($k = 0$) can result in much better blocking than the AIP strategy.

[2] We chose our range for ω based on the folk-rule which states that "handoff dropping is ten times worse than new call blocking."

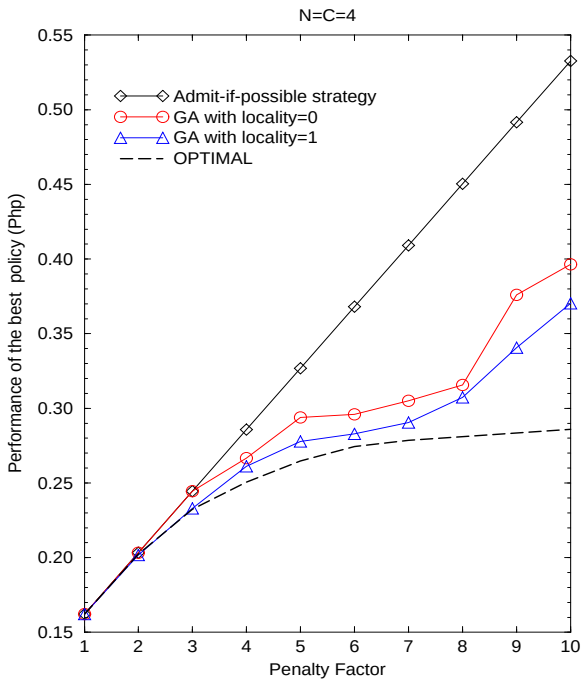

Figure 1: Comparison of Local policy performances to AIP strategy results and the optima. $\lambda = \mu = \gamma = 1.0, \omega, \in [1, 10]$

As ω gets larger, local policy performance degrades relative the optimal. We believe this phenomenon is attributable to a need for information about potential handoffs in distant cells about which the local policy has no knowledge.

The new call blocking and handoff dropping probabilities of the best policies are shown in Figures 2 and 3. The AIP strategy has fixed performances whereas the optimal policy and the policies found by GA tend to increase the new call blocking and favor the handoffs. While the GA found $k = 1$ local policies which do not suggest any regular structure, the $k = 0$ policies found are handoff reservation policies with half of the channels (2 channels) reserved for handoffs for $\omega \geq 5$.

The second set of experiments use fixed loading and penalty factor. In Figure 4, the best performances are found for different handoff rates, γ, using the AIP strategy, GA with $k = 0$ and 1, and compared to the optimal values found by MDP. The exact parameter values are:

$$\lambda = \mu = \rho = 1.0 \qquad \omega = 6$$
$$\gamma \in \{0.1, 0.2, 1.0, 2.0, 3.0, 5.0, 10.0, 20.0\}$$

It is again observed that the GA-derived policies with $k = 0$ and 1 outperform the AIP strategy by a substantial amount and are close in performance to the MDP optimum. The performance using more network information ($k = 1$ vs. $k = 0$) appears to be better, but the gain is not very substantial. As with the variable ω

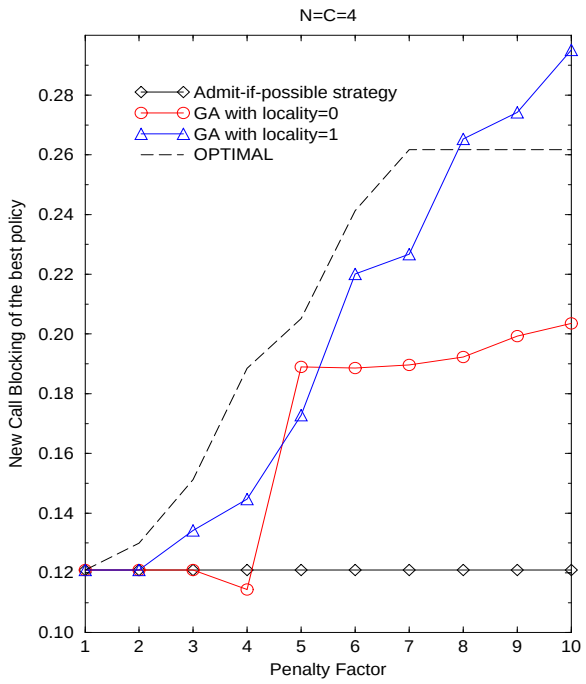

Figure 2: New Call Blocking Performances of the policies for the 4-cell 4-channel system

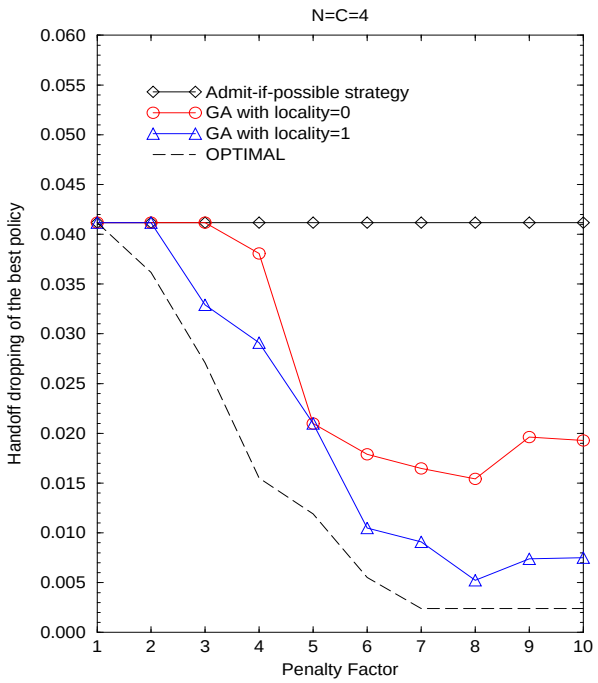

Figure 3: Handoff Dropping Performances of the policies for the 4-cell 4-channel system

case, better policies (both GA and the optimal) reduce the handoff dropping at the expense of blocking more new calls and begin to degrade as knowledge about potential handoffs in distant cells becomes more important (with increasing γ).

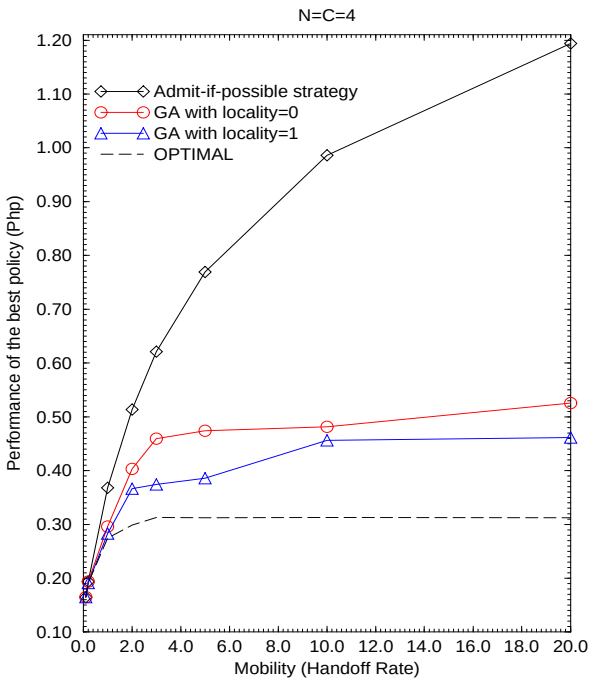

Figure 4: Comparison of the Local policy performances to AIP strategy results and the optima with different mobility rates. $\lambda = \mu = 1, \omega = 6$

5.2 16-cell System

Next, we consider a larger system with 16 cells and 9 channels. As explained in Section 3, the number of states in the system in on the order of 10^{16}. Since this exceeds our practical computational limits using MDP, the optimal policy performances are not available for this system.

The search for the best local policies with $k = 0, 1$ for this system is performed using the GA with the following parameters:

$$\lambda = 3.0, \qquad \mu = 1.0, \qquad \omega = 6, \qquad \gamma = 1, 2, ...5$$

The resulting performances of the best policies found by GA are compared to the AIP strategy in Figure 6. In addition, the best handoff reservation policy for this system for each different mobility measure was found using exhaustive search. The handoff reservation policies are defined in the following fashion:

$$D(s) = \begin{cases} 1 & \text{if } s < t \\ 0 & \text{if } s \geq t \end{cases} \tag{3}$$

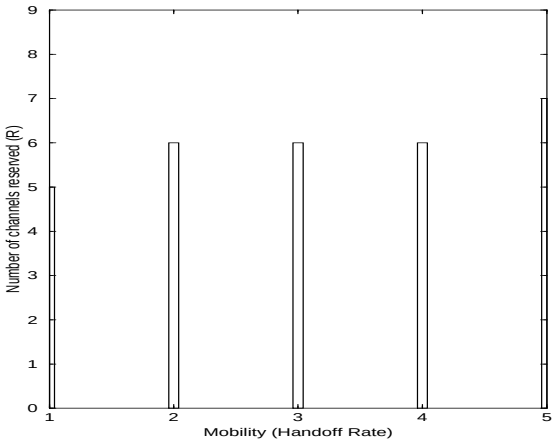

Figure 5: Structure of optimum Handoff reservation policies found for the 16-cell, 9-channel system. A new call is not admitted to the system beyond a certain threshold T.

where s is the cell occupancy (state). $D(s)$ is the decision, admit (1) or reject (0), made by the policy when the cell has s active calls, and t is the threshold beyond which no new call request will be accepted to the cell. The optimal reservation policy thresholds are shown in Figure 5. The performances of these reservation policies are compared to those for GA-derived local policies in Figure 6.

As with the smaller system, we see that both local policies provide better performance than the AIP strategy. One also expects the local policy search with $k = 1$ to outperform the handoff reservation policies since providing more information cannot degrade optimal policy performance. Specifically, consider that handoff reservation is actually a local policy with $k = 0$; the admission decision is made solely on the basis of cell occupancy and neighbors are ignored.

Note however, that the GA-derived $k = 0$ policy also outperforms the best handoff reservation policy. This result is somewhat surprising since as a general rule, reservation policies often achieve near-optimal performance. To see if the results might be explained by morphological features of the GA-derived polices, we examined the policy structure. The following double threshold of form was observed;

$$D(s) = \begin{cases} 1 & \text{if } s < t_1 \\ 0 & \text{if } t_1 \leq s < t_2 \\ 1 & \text{if } s \geq t_2 \end{cases}$$

as opposed to a single threshold reservation policy defined in Equation 3. Here t_1 and t_2 are the thresholds. For all different mobility rates, the structure of the best local policy with $k = 0$ tends to admit any service request when the cell is not very busy, blocks the new call requests when the cell is moderately busy, and services all requests when the cell is nearly full.

A moment's though reveals some method to the madness. When the cell is nearly empty and moderately loaded, little is known about the state of neighboring cells and the potential for blocked handoff requests. Thus, the most advisable course is to institute a reservation policy. However, when a cell is nearly full, the reuse constraints require that nearby cells be lightly loaded. This translates into a reduced potential handoff load. Thus, it is advisable to again allow admission to new calls.

More precisely, assume that a cell state n_i is close to the total number of available channels C. Now note that a valid channel assignment for the network is possible only when [11]:

$$n_{i-1} + n_i \leq C \qquad and \qquad n_i + n_{i+1} \leq C$$

So, if $n_i = C - r$, n_{i-1} or n_{i+1} can have at most r active calls. When r is small, cell i is nearly full and the neighboring cells must be nearly *empty*.

The incoming handoff rate to cell i from the neighboring cells is given by:

$$\Gamma = n_{i-1}(0.5\gamma) + n_{i+1}(0.5\gamma) = \gamma(n_{i-1} + n_{i+1})/2$$

$$\Gamma \leq \gamma r$$

Thus, when r is small, Γ (and therefore probability of having a handoff in time Δt, $\Gamma \Delta t$) is small. Now notice that the handoff reservation policy in this case still reserves the channel for an event that is not very probable at the expense of rejecting new calls. The GA-derived policies however, suggest allowing access to new call requests when handoffs are improbable and this results in better performance.

6 Conclusion

We have considered the local call admission problem for ring-structured cellular networks with two types of service (new call set up and handoff). The system performance measure is defined as a linear combination of new call blocking and handoff dropping probabilities of the network.

To derive policies which minimize this measure, we have used local state-based call admission policies when the optimal policy cannot be found due to computational limitations of MDP method. The search for these local policies is done by a Genetic Algorithm.

It was shown that for small systems, local policies performed nearly as well as MDP-derived optimal policies. Since MDP was impractical for larger systems, we used GA to find good admission policies and compared the

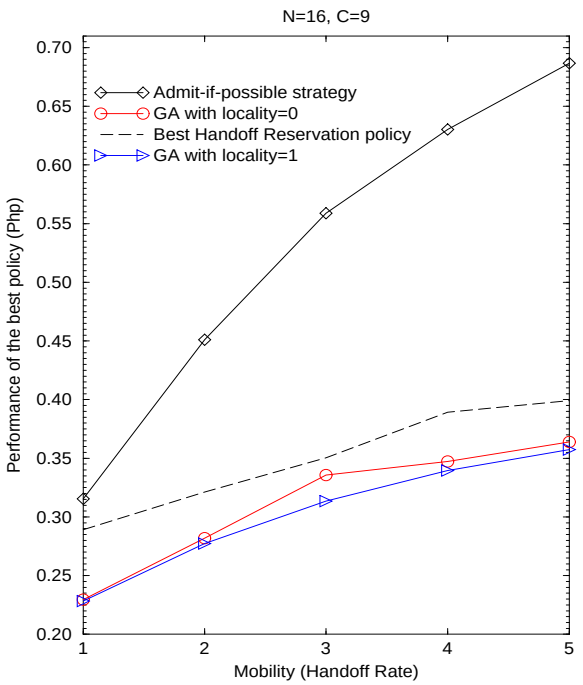

Figure 6: Comparison of the Local policy performances to AIP strategy and the optimum Handoff reservation policies found for the N=16 cell, C=9 channel system with $\lambda = 3, \mu = 1, \omega = 6$

results to the well-known methods of maximum packing and handoff reservation. The local policies outperformed the maximum packing strategy as well as the best handoff reservation policies. Most striking was the GA ability to identify a novel policy structure which made use of the inherent correlations imposed on neighboring cell occupancy by channel reuse constraints. This result bodes well for the use of GAs as an aid to analytic intuition.

Finally, we note that from the convergence point of view, the best local policies with $k = 0$ were found much more readily than for $k = 1$.[3] We also note that implementation of $k = 1$ policies would require additional intercell signaling. Coupled to the meager improvement afforded by increasing k from zero to one over the range of handoff blocking weights ω and mobilities γ considered, policies which base their decisions only on single cell occupancy might prove attractive.

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[3] The policy space size was 2^{30} for $k = 0$ as compared to 2^{3000} for $k = 1$.